Activity Recognition with Multi-tape Fuzzy Finite Automata

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Abstract — Recognizing the activities performed by the user in an unobtrusive manner is one of the important requisites of pervasive computing. Users perform a number of activities during their day to day life. Tracking and deciding what a user is doing at a given time involves a number of challenges. The lack of a precise pattern in doing an activity at different times is one among them. The number, order, and duration of the different steps involved in an activity vary significantly, even when the activity is done by the same user at different times. To overcome these challenges, a number of simultaneous inputs have to be handled with provisions for handling variations in number, order and duration of these inputs. This paper explains how multi-tape fuzzy finite automata can be used to effectively recognize human activities. The method explained is found to give good results when tested using publicly available activity datasets collected in a smart home environment.

Index Terms — Pervasive Computing, Activity Recognition, Fuzzy Automata

I. INTRODUCTION

The ability to recognize human activities automatically and unobtrusively in a smart environment has a number of applications varying from essential services such as healthcare and security to luxurious services such as automatically adjusting room ambience and ergonomics[1][2][3]. A smart environment usually has a large number of different types of sensors embedded in almost every possible component of the environment. These sensors provide input about the user’s interaction with the environment. Using these inputs the activity recognition system has to decide and possibly predict the activity performed by the user. This decision or prediction may then be used by some other larger system to provide appropriate services to the user. The task of activity recognition gets complicated by the need to handle many simultaneous sensor inputs and the impreciseness with which users perform activities. A number of probabilistic and structural methods have been developed by researchers to recognize activities [4] - [19]. This paper illustrates how multi-tape fuzzy finite automata can be used for recognizing human activities. The multi-tape feature will be useful in representing multiple simultaneous inputs; and the concept of fuzziness can be used to represent and deal with the variations in the pattern of human activities. The method is found to produce results that are comparable to other frequently used methods.

The remainder of this paper is organized as follows: Section II presents an overview of the related works in activity recognition; section III defines the problem statement; section IV presents the fundamental concepts of multi-tape automata and fuzzy automata; section V explains the proposed method; section VI discusses the dataset used and the experiment conducted; and section VII presents conclusion.

II. RELATED WORK

In their attempt to develop a framework for solving the problem of activity recognition, researchers have used a number of models. Among them, the Hidden Markov Model (HMM) is the most commonly used. Sanchez, D. et al. [1] trained a discrete HMM to map contextual information to a user activity. The model was trained and evaluated using data captured from 200 hours of detailed observation and documentation of hospital workers. Tim van Kasteren et al. [2] recorded a dataset consisting of 28 days of sensor data in a smart home environment and through a number of experiments showed how the HMMs perform in recognizing activities. An approach for multi-person activity recognition in an office environment using audio as well as video features, employing a multilevel HMM framework is used by Christian Wojek et al. [3]. Human activities embedded in video sequences acquired
in an archeological site are automatically recognized using Discrete HMMs by Marco Leo, et al. [4]. Weiyao Huang, et al. [5] used Discrete HMM for human posture training, modeling and activity matching to recognize human motion. Other HMM variations such as Coupled HMM, Fuzzy HMM, Hierarchical HMM and Reconfigurable HMM are used by other researchers [6] [7] [8] [9].

Rocío Díaz de León et al. [10] used a Bayesian network for recognition of continuous activities, by considering the direction change between frames to track the motion of several limbs and to recognize different activities. An approach for human activity recognition that can recognize activities performed at different velocities by different people and can work with missing data, based on the Fourier transform and Bayesian networks was presented by Rocío Díaz de León [11]. A system that uses naïve Bayesian classifier for recognizing activities in the home setting using a set of small and simple state-change sensors is introduced by E.M. Tapia, et al. [12]. In the framework suggested by Sangho Park and J.K. Aggarwal [13], human action is represented in terms of verbal description according to subject + verb + object syntax, and human interaction is represented in terms of cause + effect semantics between the human actions. Then, a dynamic Bayesian network is constructed to estimate temporal evolution of the human actions for recognizing the dynamic gestures of the body parts. Tim van Kasteren and Ben Kröse [14] used a Dynamic Bayesian Network, to model the temporal aspects of the activities of daily living (ADL) of elders. They observed that adding more sensors does not necessarily increase accuracy. A multi-level dynamic Bayesian network was used to perform complex event recognition by Justin Muncaster and Yunqian Ma [15]. The levels of the network are used to enforce state hierarchy while the lowest level models the duration of simplest event. The probability that a scenario occurs is computed from the mobile object properties obtained from a sequence of image frames using several layers of naïve Bayesian classifiers in the work presented by Somboon Hongeng, et al. [16].

Friedrich Steimann and Klaus-Peter Adlassnig presented a framework for an intelligent bedside monitor that derived an abstraction of the current status of a patient by fuzzy state transitions on pre-processed input supplied continuously by clinical instrumentation [17]. This is one of the earlier works that use fuzzy automata for activity recognition. A Fuzzy Rule based Classifier and two Fuzzy Finite State Machines (FFSM) are used by A. Alvarez-Alvarez, et al. [18] to recognize activities like working in the desk room, crossing the corridor, having a meeting, etc. The classifier is used to get an approximate position at the level of discrete zones such as office, corridor and meeting room. One of the FFSM is used for human body posture recognition and the other FFSM combines the localization and posture recognition. The use of fuzzy finite state systems is demonstrated in [19] for human gait modeling. Gonzalo Bailador and Gracián Triviño [20] propose a syntactic pattern recognition approach based on fuzzy automata, which can cope with the variability of patterns by defining imprecise models. The approach is called temporal fuzzy automata as it allows the inclusion of time restrictions to model the duration of the different states. This approach is used for recognizing hand gestures.

Though the above works use fuzzy automaton to deal with variability and impreciseness of human activities, the states of the fuzzy automata are manually defined by an expert. This will be tedious, as the number of states becomes very large. So in this paper we propose to use an algorithm suggested by Henning Fernau [21] to automatically construct a DFA to recognize human activities using a set of sensor inputs, represented as strings. Then the concept of fuzziness is introduced by using appropriate functions to deal with variability and impreciseness of human activities. The proposed method is tested with a publicly available data set, and the results are comparable to other commonly used methods.

III. THE PROBLEM

The objective is to recognize activities from sensor readings in a smart environment. For this, the time series data of sensor readings is divided into time slices of constant length. Each time slice is labeled with the activity performed during that time slice [2]. A vector \( \bar{x}_t = (x_1^t, x_2^t, \ldots, x_n^t) \) is used to represent the sensor readings at time slice \( t \), where \( x_i^t \) represents the input from the sensor \( x_i \) during the time slice and ‘\( N \)’ is the number of sensors. The activity performed during time slice ‘\( t \)’ is represented by \( y_t \). So, the task of the activity recognition system is to find an association between a sequence of observation vectors \( x = \{ \bar{x}_1, \bar{x}_2, \ldots, \bar{x}_n \} \) and a sequence of activity labels \( y = \{ y_1, y_2, \ldots, y_n \} \). Fig.1 illustrates the above setup, with \( \Delta t \) representing a time slice.
IV. MULTI-TAPE FINITE AUTOMATA

A two-way finite-state automaton with \( n \geq 1 \) tapes scans \( n \) read-only input tapes, each with an independent head [22]. At every step, the transition function determines the possible next states and head movements, based on the current state and the symbols currently under each head. Two special symbols \( \alpha, \beta \) respectively mark the left and right ends of each input tape; \( \Sigma_{n,a} \) denotes the extended alphabet \( \Sigma \cup \{ \alpha, \beta \} \).

![Time Slices and States](image)

**Definition**: A two-way nondeterministic finite-state automaton with \( n \) tapes is a tuple \( (\Sigma, Q, \delta, q_0, F) \), where :

- \( \Sigma \) -- is the input alphabet, such that \( \alpha, \beta \notin \Sigma \);
- \( Q \) -- is the finite set of states;
- \( \delta : Q \times \Sigma_{n,a}^* \rightarrow \varnothing(Q \times \{-1, 1, 0\}^n) \) is the transition function that maps current state and input to a set of next states and head movement directions, with the restriction that the head does not move beyond the end markers;
- \( q_0 \in Q \) is the initial state;
- \( F \) a subset of \( Q \), is the set of accepting states.

The configuration of a two-way nondeterministic finite-state automaton \( A \), is defined as a \((2n+1)\)-tuple,

\[
(x_1, \ldots, x_n, q, i_1, \ldots, i_n, q', i'_1, \ldots, i'_n)
\]

if and only if, for each \( 1 \leq k \leq n \), \( x_k \) is the content of the \( k \)-th tape and \( 0 \leq i_k \leq |x_k| \) is the position of the \( k \)-th head; when \( i_k = 0 \) (resp. \( i_k = |x_k| + 1 \)) the head is on the left marker \( \alpha \) (resp. right marker \( \beta \)).

The transition relation \( \vdash \) between configurations is defined as:

\[
(x_1, \ldots, x_n, q, i_1, \ldots, i_n) \vdash (x_1, \ldots, x_n, q', i'_1, \ldots, i'_n)
\]

An accepting run \( \rho \) of \( A \) on input \( x \) is a sequence of configurations \( X_0 \ldots X_m \) such that \( X_0 = (x, q_0, 0^n) \) and for all \( 1 \leq k \leq m, X_{k-1} \vdash X_k \). A run \( \rho \) of \( A \) on input \( x \) is accepting if \( X_m = (x', q, 1, \ldots, 1) \) for some \( q \in F \) and the character of the \( k \)-th tape is \( \alpha \) (that is, every head has reached the end of its tape). Correspondingly, \( A \) accepts an input word \( x \) if there is an accepting run \( \rho \) of \( A \) on \( x \). The language accepted by \( A \) is the set of \( n \) words \( L(A) = \{ x \in (\Sigma^n)^n / A \text{ accepts } x \} \).

An \( n \)-tape automaton \( A \) is deterministic if \( |\delta(q, \sigma_1, \ldots, \sigma_n)| \leq 1 \) for any \( q, \sigma_1, \ldots, \sigma_n \). Further, an \( n \)-tape automaton is said to be \( s \)-synchronized for \( s \geq 0 \) if every run of \( A \), accepting or not, is such that any two heads that are not on the right-end marker \( \alpha \) are no more than \( s \) positions apart (as measured from the left-end marker \( \beta \)). And, \( A \) is said to be \( s \)-synchronized if it is \( s \)-synchronized for some \( s \in \mathbb{N} \). A is simply synchronous if it is 0-synchronized. If the mapping \( \delta \) never moves any of the heads left, then \( A \) is said to be one-way.

One-way, synchronous \( n \)-tape finite automata are closed under complement, intersection, union, concatenation, Kleene closure, projection, generalization, and reversal[22].

A. FUZZY FINITE AUTOMATA (FFA)

Besides a finite set of states(\( Q \)), a finite set of input symbols(\( \Sigma \)), and a start state(\( q_0 \)), a Fuzzy Finite Automata has a finite set of output symbols(\( Z \)), fuzzy transition function(\( \delta \)) and an output function(\( \omega \)). \( \delta : Q \times \Sigma \rightarrow (0, 1] \) is the fuzzy transition function which is used to map a current state into a next state upon an input symbol and attributing a value in the fuzzy interval \( (0, 1] \) to the next state. \( \omega : Q \times Z \rightarrow (0, 1] \) is the output function which is used to map a state to the output set. The membership value (mv) associated with each transition is called the weight of the transition [24].

One of the main differences between a FFA and a DFA(or an NFA) is that, in a FFA there can be more than one active state at a time. Each active state is associated with a membership value that indicates the level of activation of the state. To assign membership values to the next states, the mv of the current state and the weight of the transition are considered.

One of the characteristics of an FFA is that, a state may be forced to take several different membership values at the same time. This is called multi-membership. Detailed description of fuzzy finite automata can be found in [24].

V. THE METHOD

As explained in section III, the time series data of sensor readings is divided into time slices of equal length. Each time slice is labeled with the activity performed during that time slice. To model this arrangement using multi-tape finite automaton, input from each sensor is considered to be a tape of the automata. So, if there are \( n \) sensors to be considered in the environment, the finite automata will have \( n \) input tapes. The time slices may correspond to states of the automaton. The automaton will make state
transitions with each time slice, according to the mapping \( \delta \). The mapping rules as required may be defined, taking into account the interactions the user makes with the environment while performing an activity. This is illustrated in fig.2 in which a time series data obtained from three sensors \( s_1, s_2 \) and \( s_3 \) are given. The entire duration is divided into equal time slices and each slice is labeled with the state corresponding to the time slice (labels \( q_1 \) to \( q_6 \)). For the sake of simplicity the sensors are assumed to generate binary input. Sensors that generate non-binary values may be accommodated in this model by determining suitable threshold value for each possible input stage. A one-way, synchronous 3-tape finite automata \( A \), to model this can be constructed as follows:

\[
A = (\Sigma, Q, \delta, q_0, F)
\]

where

\[
\Sigma = \{0, 1\}
\]

\[
Q = \{q_0, q_1, q_2, q_3, q_4, q_5, q_6\}
\]

\( q_0 \) is the initial state \( F = \{q_6\} \)

and

\[
\delta(q_0, 000) = (q_1, 1)
\]

\[
\delta(q_1, 110) = (q_2, 1)
\]

\[
\delta(q_2, 101) = (q_3, 1)
\]

\[
\delta(q_3, 100) = (q_4, 1)
\]

\[
\delta(q_4, 010) = (q_5, 1)
\]

\[
\delta(q_5, 000) = (q_6, 1)
\]

Additional mapping conditions may be included to keep the automaton in the same state when there is no change in the inputs. Also, for each state a maximum duration may be included, after which the inputs must change to move the automaton to the next possible state; otherwise, the automaton may be moved to the initial state, so that it can be synchronized with the next possible input pattern.

In the works from the literature, the states of the fuzzy automata were decided manually by experts. This approach may not be feasible in an environment where a user may perform a single activity in a widely varied ways. The problem becomes more complicated if a large number of sensor inputs also have to be considered. So, in this work we suggest automatic construction of a finite automata that will scan the sensor input vectors and will identify the corresponding activity performed by the user. The \( S_k \)-infer algorithms suggested by Henning Fernau [21] are used by us for the automatic construction of a finite automaton. Then, appropriate functions for deciding membership values are used to incorporate the required fuzziness in the constructed automaton.

VI. DATA AND EXPERIMENT

A number of activity datasets, collected using sensors embedded in the environment and/or worn by the subjects, are publicly available. We have used one such data set collected and made public by Tim van Kasteren, et al.[23]. The datasets have been collected by observing the behavior of inhabitants inside their homes using wireless sensor networks. Output of the binary sensors have been annotated with the activities performed by the subjects during predefined time intervals. A dataset so collected for 25 days of 10 activities such as preparing dinner, using toilet and sleeping, is used by us to conduct the experiment.

Three different representations, namely raw, change point and last-fired, of the sensor data are used [23]. The raw sensor representation uses the sensor data directly as it was received from the sensors. The change point representation indicates when a sensor event takes place. The last-fired sensor representation indicates which sensor fired last. For each of the representations, six different time slices (600, 300, 60, 30, 10 and 1 seconds) have been used. Sensor data for each of the 10 activities and for each representation were culled from the data set.

A fuzzy automaton for recognizing a particular activity is constructed as follows. Each possible binary output vector in the dataset for the activity – a vector corresponding to a time slice – is assigned a unique character code. Thus a set of strings representing the time series data for the activity is generated and given as input to the DFA construction algorithm.

Fuzzy characteristic is incorporated in the generated DFA by slightly modifying the transition function. Initially the list of active states consists only of the initial state, and its membership value is set to 1.0. For each currently active state \( q \), and the content of the input tapes at time \( t \), \( x_t \), the following is done. If \( \delta(q, x_t) \) is defined by the generated automaton then the transition is carried out and the membership value of \( q \) is assigned to the next state. Otherwise, the distance between \( x_t \) and each \( x_p \), for which \( \delta(q, x_p) \) is defined, is calculated; this distance information is used to decide the membership value of the corresponding next possible active state. Naturally, a next state caused by an \( x_p \) with minimum distance from \( x_t \) has greater membership value than the one caused by the one with greater distance with \( x_t \). In short, the membership value of a next state is inversely proportional to the distance of an allowable input with \( x_t \). Lesser the distance, greater the membership value and vice versa. The problem of multi-membership is solved by choosing the maximum of the membership values.

Proceeding in this way, after the membership value of each active state for the last input in the given test string is calculated, the highest membership value of the active states is considered to decide if the given input is accepted by the FFA or not. If the highest membership value is greater than or equal to the threshold value...
specified by the user, the input is accepted by the FFA, otherwise it is rejected.

The effectiveness of the automata hinges on the method for calculating the membership values of the next states. For this we have considered the membership value of a current state \( q \) and the distance between \( x_t \) and an \( x_p \) for which \( \delta(q,x_p) \) is defined. The actual formula used is given below:

\[
mv = (0.5 \times.mvc) + (0.5 \times (1.0 - \text{dist} / \text{ns})
\]

where

\( mv \) – membership value of next state,

\( mvc \) – membership value of current state,

\( \text{dist} \) – distance between \( x_t \) and \( x_p \), and

\( \text{ns} \) – number of sensors in the environment.

The distance between \( x_t \) and \( x_p \) is calculated as the number of positions in which the two vectors differ.

As said earlier, the problem of multi-membership is solved by choosing the maximum of the newly calculated membership values of a next active state.

The performance of the built fuzzy finite automata was measured by calculating recall, precision and F-measure as follows.

\[
\text{F-measure} = \frac{2(\text{recall} \times \text{precision})}{(\text{recall} + \text{precision})}
\]

\[
\text{recall} = \frac{tp}{(tp + fn)}
\]

\[
\text{precision} = \frac{tp}{(tp + fp)}
\]

where \( tp, fp \) and \( fn \) represent the number of true positives, false positives and false negatives. Fig.3 shows the F-measures obtained for the three representations and the six time slices.

The average F-measure obtained by our method for the raw, change point and last-fired representations are 0.74, 0.76 and 0.78 respectively. There is only slight difference in the performance due to the feature representation methods. The average F-measure values are comparable to the F-measures obtained by the methods described by Kasteren, et al. [23].

VII. CONCLUSION

Relatively less attention has been paid by researchers to use fuzzy finite automata for activity recognition. In this work we have demonstrated how the automatic construction of a DFA can be used for activity recognition when combined with fuzzy concept. We plan to extend this work by incorporating the ability to recognize temporal characteristics peculiar to the given sensor input sequences.

REFERENCES


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